

Diagnostic of laser induced Li II plasma

Banaz Omar, August Wierling, Heidi Reinholz, and Gerd Röpke

Institut für Physik, Universität Rostock, Universitätsplatz 3, 18051 Rostock, Germany

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Abstract

Spectral line broadening in dense plasmas is investigated for lithium He-like ion based on a microscopic quantum-statistical approach. By using thermodynamic Greens function, perturber-radiator interaction, plasma correlation and screening effects are taken into account. Ions are treated in quasi-static approximation, leading to a Stark effect by the surrounding perturbers microfield. Stark broadening of Li II ($2p^3P_{2,1,0} - 2s^3S_1$) 548 nm line is calculated, plasma parameters such as temperature and free electron density for the expanding Li plasma after 60 ns from laser irradiation are analyzed (Doria, D., Kavanagh, K.D., Costello, J.T., and Luna, H. (2006) Meas. Sci. Technol., 17, 670-674). The estimated spatial electron density and temperature ranges are $n_e = (0.25-2) \times 10^{24} \text{ m}^{-3}$ and $T \approx (2-3.5) \text{ eV}$, respectively. The dependence of plasma parameters on the line width is investigated. A good agreement is shown by comparing our calculation with the published measured profiles.

Keywords: Stark broadening; Greens function; plasma diagnostic

2010 Mathematics Subject Classification: 53C25; 83C05; 57N16

1 Introduction

Spectral line calculation is an interesting tool for plasma diagnostic. A radiating atom in dense plasmas is perturbed by the influence of surrounding particles, the perturbation leads to the shift and broadening of the line profile, the most dominating effect is Stark broadening. The diagnostic of the spatial and temporal distribution of plasma parameters in a laser-produced plasma is of great interest to many fields in science. Spectral line broadening of Li has industrial applications, lithium is used as a sources for EUV lithography and for soft x-ray emission. The plasma parameters, such as free electron density and temperature can be determined directly from calculated line profile in dense plasmas [Griem (1974)]. The temperature and density distributions are useful for fabrication of thin film materials such as high-temperature superconductors [Bäuerle (1998)].

In this paper we analyze the experimental result of laser-produced Li II plasma at time delay 60 nm, the experiment have been carried out by Doria et al. [Doria et al. (2006)]. Time and

*Corresponding author: E-mail:banaz.omar@uni-rostock.de

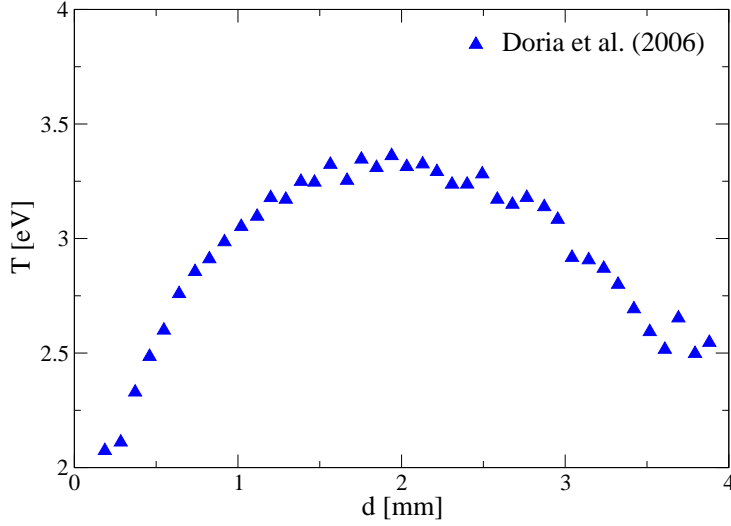


Figure 1: Spatial temperature profile of Li II in one dimension after 60 ns time delay, estimated in Ref. [Doria et al. (2006)].

spatially resolved spectra is measured in one dimension along the plasma expansion normal to a Li target by using a time gated intensified charge-coupled device (ICCD) coupled to a stigmatic spectrometer. A Q-switched Nd:YAG laser at $\lambda = 1064$ nm is used with pulse duration 15 ns and 10 Hz repetition rate, the laser is focused onto a pure Li sample surface placed inside a vacuum chamber (5×10^{-5} mbar) generating a plasma that expands normal to the target surface. The laser irradiance is kept constant at an average of 1.3×10^{10} W cm². Laser-induced plasma parameters such as electron temperature, density and plume velocity are extracted directly from the image analysis which has been automated using a MATLAB code. The technique permitted rapid and ready characterization of laser plasma plumes in the early stage of the plasma expansion [Doria et al. (2006)]. The temperature is determined from line intensity ratio of successively charged ions, which is the widely used technique. The spatial profile of the electron density is also estimated by using semiclassical perturbation formalisms from standard theory (ST) of Griem [Griem (1974)]. The ST is a semiclassical approach, where electrons are treated by using impact approximation with a cut-off procedure, while the interaction of ions at radiating particle is given in a quasi-static approximation due to the static microfield distribution function.

The quantum-mechanical Greens function method is considered in this paper to calculate the Li II spectral lines in dense plasmas, assuming local thermal equilibrium (LTE) [Kraeft et al. (1986); Günter and Könies (1994); Sorge et al. (2000); Omar et al. (2006)]. In Sec. 2 an overview of the spectral line modeling is given. Result and discussion are shown in Sec. 3. Comparison with the experimental results of Doria et al. [Doria et al. (2006)] is presented. Finally, conclusion is given in Sec. 4.

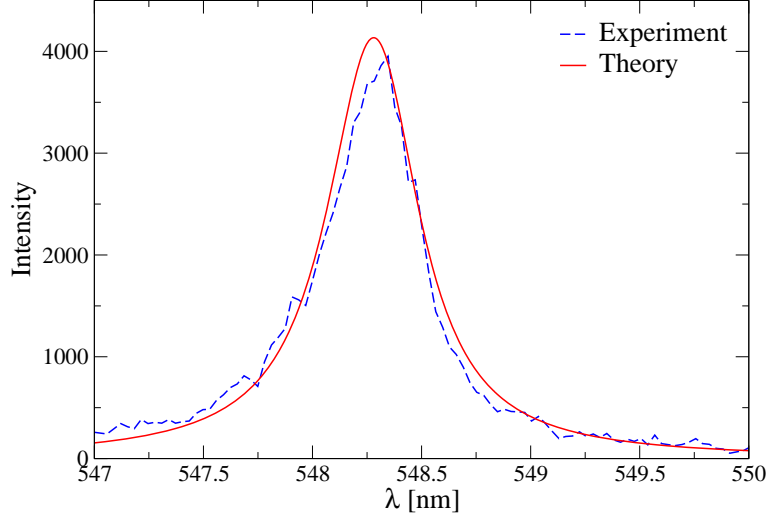


Figure 2: Pressure broadening of the line 548 nm Li II versus wavelength, theoretical profile at $n_e = 1.6 \times 10^{18} \text{ cm}^{-3}$ compared with the measurement [Doria et al. (2006)] at $n_e = 1.885 \times 10^{18} \text{ cm}^{-3}$, $T = 2.46 \text{ eV}$, and $d = 0.43 \text{ mm}$.

2 Theoretical approach of pressure broadening in dense plasmas

Spectral line shape is given by the second order two-particle polarization function, which is a bound-bound transition. The polarization function is calculated in a systematic way from thermodynamic Greens function, which is proportional to the Fourier transform of the dipole-dipole autocorrelation function. The perturber-radiator interaction leads to a **pressure broadening**, which contains an electronic and an ionic contributions. Including the ionic contribution in the quasi-static approximation by averaging over the ionic microfield [Sorge et al. (2000)], we have

$$I^{\text{Br}}(\omega) \sim \sum_{i', i'', f', f''} \langle i' | \mathbf{r} | f' \rangle \langle f'' | \mathbf{r} | i'' \rangle \frac{\omega^4}{8\pi^3 c^3} e^{-\frac{\hbar\omega}{k_B T}} \int_0^\infty W(\beta) d\beta \\ \times \text{Im} \langle i' | \langle f' | [\hbar\omega - \hbar\omega_{if} - \Sigma_{if}(\omega, \beta) + i\Gamma_{if}^v]^{-1} | f'' \rangle | i'' \rangle , \quad (2.1)$$

where $\langle i | \mathbf{r} | f \rangle$ is identified as a **dipole matrix-element** for the transition between **initial** $n_i l_i m_i$ and **final** $n_f l_f m_f$ **states**. The **vertex correction** Γ_{if}^v for the overlapping line is related to coupling between the initial and the final states [Kraeft et al. (1986)]. The **ionic microfield distribution function** $W(\beta)$ is taken according to Ref. [Hooper (1968)] with **field strength** $\beta = E/E_0$ normalized to the **Holtmark field** E_0 , and $\hbar\omega_{if} = E_i - E_f$ is the **unperturbed transition energy**. The function $\Sigma_{if}(\omega, \beta)$ is determined by the **self-energy correction** $\Sigma_n(\omega, \beta)$ of the **initial and the final states**

$$\Sigma_{if}(\omega, \beta) = \text{Re}[\Sigma_i(\omega, \beta) - \Sigma_f(\omega, \beta)] + i \text{Im}[\Sigma_i(\omega, \beta) + \Sigma_f(\omega, \beta)] , \quad (2.2)$$

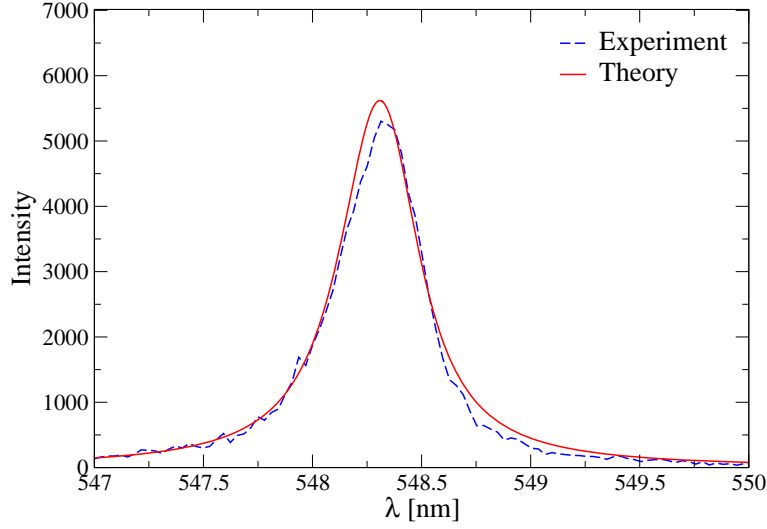


Figure 3: The calculated line profile of Li II 548 nm versus wavelength at $n_e = 1.376 \times 10^{18} \text{ cm}^{-3}$ and $T = 2.58 \text{ eV}$. Comparison is made with the measured line [Doria et al. (2006)] at estimated electron density $n_e = 1.38 \times 10^{18} \text{ cm}^{-3}$ and distance $d = 0.53 \text{ mm}$.

where the real part represents the shift Δ_n^{SE} and the imaginary part gives the width Γ_n^{SE} of each state. The electronic and ionic contributions occur in the self-energy

$$\Sigma_n(\omega, \beta) = \Sigma_n^{\text{ion}}(\beta) + \Sigma_n^{\text{el}}(\omega, \beta) . \quad (2.3)$$

Performing Born approximation with respect to the dynamically screened perturber-radiator potential, the electronic self-energy is obtained as

$$\begin{aligned} \Delta_n^{\text{SE}} + i\Gamma_n^{\text{SE}} &= \langle n | \Sigma^{\text{el}}(E_n, \beta) | n \rangle = -\frac{1}{e^2} \int \frac{d^3q}{(2\pi)^3} V(q) \sum_{\alpha} |M_{n\alpha}(\mathbf{q})|^2 \\ &\times \int_{-\infty}^{\infty} \frac{d\omega}{\pi} [1 + n_B(\omega)] \frac{\text{Im} \varepsilon^{-1}(\mathbf{q}, \omega + i0)}{E_n - E_{\alpha}(\beta) - \hbar(\omega + i0)} . \end{aligned} \quad (2.4)$$

Here, the level splitting ($E_{\alpha}(\beta) \approx E_{\alpha}$) due to the microfield has been neglected [Günter and Könies (1994)], $n_B(\omega) = [\exp(\hbar\omega/k_B T) - 1]^{-1}$ is the Bose distribution function, and the sum over principal quantum number α runs from $n-2$ to $n+2$ discrete bound states for the virtual transitions. Dynamical screening effect is accounted for in Eq. (2.4) from imaginary part of the inverse dielectric function $\varepsilon^{-1}(\mathbf{q}, \omega)$, which is approximated by random phase approximation (RPA). The transition matrix-element $M_{n\alpha}(\mathbf{q})$ describes the interaction of the atom with the Coulomb potential through the vertex function, where the Coulomb interaction with electron-electron-ion triplet depends on the momentum transfer $\hbar\mathbf{q}$ [Kraeft et al. (1986)]. The matrix-element of He and He-like ions can be approximated by the one of hydrogen, while the outer electron is screened by inner electron [Omar et al. (2006)]. The electronic wavefunction for singly ionized Li is obtained by applying Coulomb approximation method [Bates and

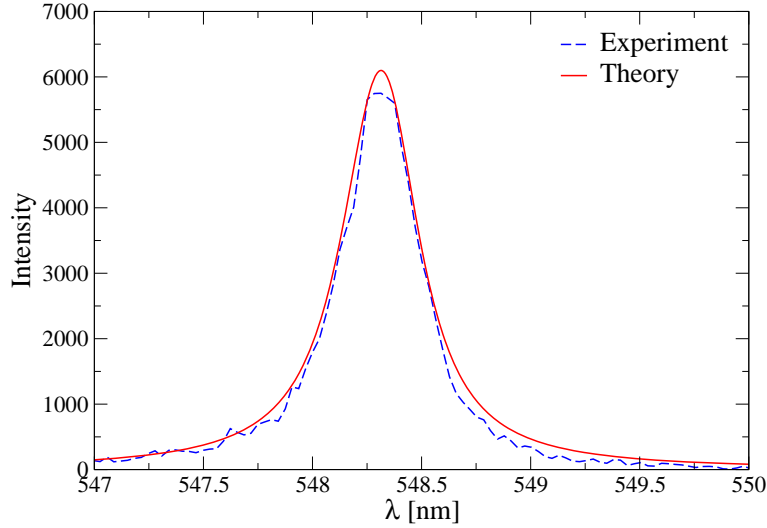


Figure 4: The calculated line shape of Li II 548 nm vs. λ at $n_e = 1.35 \times 10^{18} \text{ cm}^{-3}$ and $T = 2.69 \text{ eV}$. Comparison is made with the measured profile in Ref. [Doria et al. (2006)] at $n_e = 1.402 \times 10^{18} \text{ cm}^{-3}$ for the same temperature at distance $d = 0.6 \text{ mm}$.

Damgaard (1949)]. In this approximation the **wavefunction and radial part of the transition matrix-element** are expressed in terms of $[P_{nl}(r) = r \psi_{nl}(r)]$ and σ , respectively. To verify the wavefunction, the **absorption oscillator strength** of transition f_{if} and σ^2 of the singly excited states of Li II are indicated as [Wiese and Fuhr (2009); **Bethe (1977)**; Cohen and Kelly (1967); Theodosiou (1985)]

$$f_{if} = \frac{1}{3} \frac{\Delta E}{R} \frac{\max(l_i, l_f)}{2l + 1} \left(\int_0^\infty r P_{n_i l_i}(r) P_{n_f l_f}(r) dr \right)^2, \quad (2.5)$$

where R is the **reduced mass Rydberg** constant, and ΔE is **the transition energy**.

Considering Born approximation, the electronic part is overestimated, to avoid this we apply the cut-off procedure and add a strong collision term [Griem (1974, 1988); Griem et al (1990)] in stated of partial summation of the three-particle T-matrix, where the result might be slightly modified. For Li II we adopt the **cut-off parameter** $\rho_{\min} = n^2/Z$, where Z is **the effective charge** [Griem (1988)]. The **close electron-radiator collision term** ϕ_{SC} is evaluated according to the semiclassical estimation in Refs. [Griem (1988); Griem et al (1990); Griem et al. (1979); Nguyen et al. (1986)]

$$\phi_{\text{SC}} = -\frac{4\pi}{3} \left(\frac{2m_e}{\pi k_B T} \right)^{1/2} n_e \left(\frac{\hbar}{m_e} \right)^2 |< nl|r|nl >|^2 C_{nl}, \quad (2.6)$$

where C_{nl} is the **strong collision constant** and $< nl|r|nl >$ is the **dipole matrix-element**.

For non-hydrogenic radiator, ionic contribution to the self-energy is related to quadratic Stark effect and quadrupole interaction, further detail is given in Refs. [Sorge et al. (2000); Omar et al. (2006)]. The microfield can be considered as a static microfield distribution function, while it does not change during the time of interest for the radiation process.

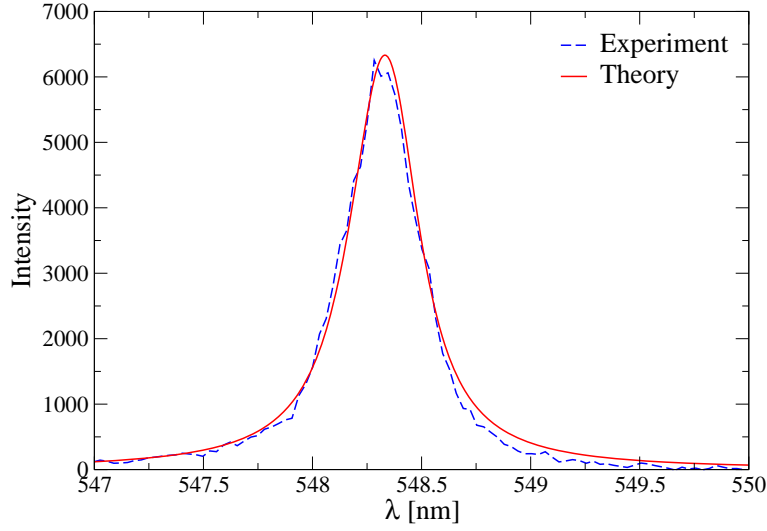


Figure 5: Stark broadening of the Li II line 548 nm versus wavelength. The calculated profile at $n_e = 1.2 \times 10^{18} \text{ cm}^{-3}$ compared with the measured one at $n_e = 0.982 \times 10^{18} \text{ cm}^{-3}$, $T = 2.77 \text{ eV}$ and $d = 0.676 \text{ mm}$ [Doria et al. (2006)].

3 Result and Discussion

In this section, we perform the pressure line broadening and the related full width at half maximum (FWHM) of the Li II 548 nm line by applying the approach outlined above. The comparison between our theoretical calculation and experimental results is shown, assuming LTE. The time-resolved measured profiles are space resolved along the direction of expansion, the observed plasma parameters such as relative line intensities and Stark broadening parameters have been extracted from the profiles [Doria et al. (2006)]. Under the assumption of LTE, the spatial electron temperature profile is evaluated from the intensity ratio of Li II at two isolated lines 548 nm and 467 nm, see Fig. 1 [Doria et al. (2006); Griem (1964)]. The relative intensities are corrected according to the wavelength dependence of the spectral sensitivity of the spectrometer. The statistical error in the intensity ratio is less than 3% for distances between $d = 1 \text{ mm}$ to $d = 3 \text{ mm}$ from the sample surface, but increased up to 10% further away at the edges of the plasma plume, where distance $d = 0$ at the target surface. Considering an initial plasma temperature of 8.6 eV gives the velocity of $1.99 \times 10^5 \text{ cm/s}$ at 60 ns time delay. The spatial distribution of the density ratio between Li ions and atoms is obtained in Ref. [Doria et al. (2006)] by using the Saha equation. Two different regions can be defined, $d < 2 \text{ mm}$ and $d > 2 \text{ mm}$ where the electron temperature reaches its maximum value, see Fig. 1. The first region is a sharp transient in the $n_{\text{ion}}/n_{\text{atom}}$ density ratio, mostly driven by the change in the electron density. However, in the second region the density ratio becomes constant, indicating that the plasma has reached thermal equilibrium between the ion and atom populations, while in this stage the electron density is almost constant and the temperature begins to drop, for more detail see Ref. [Doria et al. (2006)].

Stark broadening parameters are calculated from Eq. 2.4 by using thermodynamic Greens

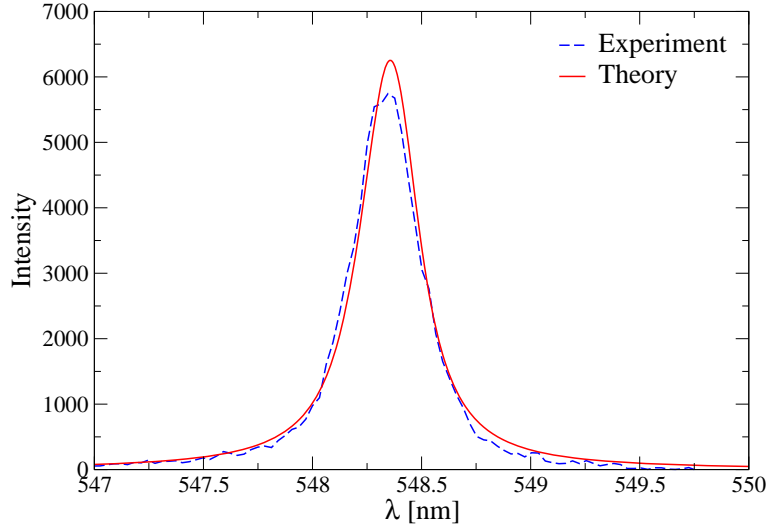


Figure 6: Comparison of the theoretical and measured line shapes of the Li II 548 nm line vs. wavelength at $n_e = 1.0 \times 10^{18} \text{ cm}^{-3}$ and $n_e = 0.962 \times 10^{18} \text{ cm}^{-3}$, respectively, at $T = 2.96 \text{ eV}$ and $d = 0.89 \text{ mm}$ [Doria et al. (2006)].

function, the cut-off procedure is adopted and the strong collision term is added by using Eq. 2.6 according to Griem and his collaborators [Griem (1988); Griem et al (1990)]. The ionic contribution is taken into account from second-order perturbation theory which is known as the quadratic Stark effect [Bethe (1977)]. Ions are treated in quasi-static approximation by using microfield distribution function of Hooper [Hooper (1968)], the comparison is done with the distribution function given in Ref. [Sadykova et al. (2009)], where no sensible difference has been observed. The pressure line broadening is evaluated from Eq. 2.1 and compared with the measurement [Doria et al. (2006)], given in Figs. 2-8. Then the electron density and the FWHM are estimated from the best-fitting profile with the measurement, illustrated in Figs. 9 and 10, respectively. The plasma expands freely and cooling down while the electron density decreases with increasing d normal to the surface. The gradient of density as a function of d in one dimension after 60 ns of laser exposure is shown in Fig. 9. The electron density profile is indicated in Ref. [Doria et al. (2006)] from line broadening by extrapolating the tabled values of Griem [Griem (1974)]. The highest value of the electron density observed near the target surface, by plasma cooling n_e decreases rapidly with increasing d due to condensation and recombination. In Fig. 9 the variation of n_e near the surface is in a good agreement with the estimation in Ref. [Doria et al. (2006)], while the discrepancy can be seen with increasing d , this can be clearly seen in Fig. 8. The first region is a transient region, rapid change in electron density can be seen and the second part is related to the plasma equilibrium, where n_e is almost constant. The Doppler broadening becomes less important with increasing density, and the width is only due to Stark broadening at high density. Regarding the data reported in Ref. [Doria et al. (2006)], the discrepancy may be due to the self-absorption.

The accuracy of calculating electronic dipole matrix-elements is approved by comparing our results of the radial part of transition matrix-element σ^2 and the oscillator strength of transition f_{if}

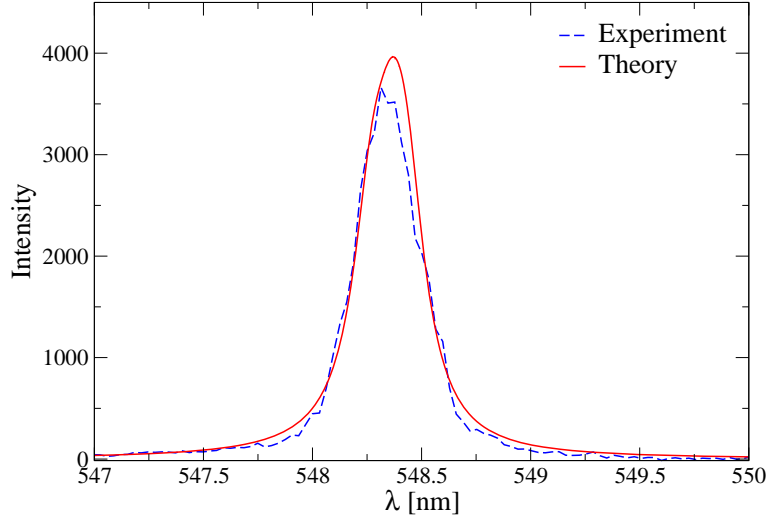


Figure 7: The line profiles of Li II 548 nm line versus wavelength. Our calculation at $n_e = 0.8 \times 10^{18} \text{ cm}^{-3}$ compared with the profile measured in Ref. [Doria et al. (2006)] at $n_e = 0.561 \times 10^{18} \text{ cm}^{-3}$, $T = 3.3 \text{ eV}$, and $d = 1.53 \text{ mm}$.

with the other calculated values in Ref. [Theodosiou (1985); Cohen and Kelly (1967); Ateş and Çelik (2009)], see table 1, very good agreement can be seen.

4 Conclusions

In this study, diagnostic of laser induced lithium plasma by Doria et al. [Doria et al. (2006)] is performed. The quantum statistical approach is presented to the line profile calculation of allowed isolated Li II 548 nm, this method is applicable for both allowed and forbidden radiative transitions. A cut off procedure is used for strong collisions according to Griem [Griem (1974)]. The Coulomb approximation is employed to evaluate the wavefunctions of Li II. In our calculation, the time-dependent microfield fluctuation is approximated by its static value due to the large mass of the ion relative to the electron mass, assuming the stationary motion of ions during the time of collisions. The contribution of ions is taken into account within quadratic Stark effect in the quasi-static approximation. The spatial distribution of the electron density is estimated along the direction of plasma plume expansion. Good agreement can be clearly seen by comparing our line profiles with the measured profiles. However, the estimated values of n_e in Ref. Doria et al. (2006) are overestimated systematically with increasing distance.

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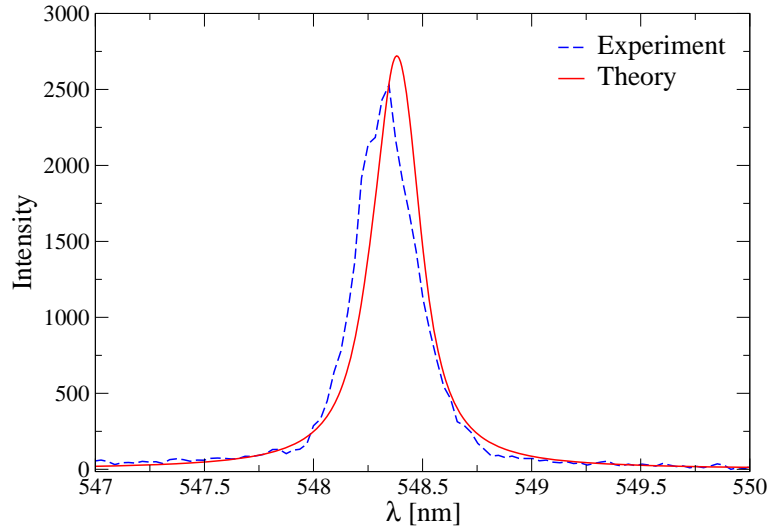


Figure 8: The line profiles of Li II 548 nm line vs. wavelength. Our calculation at $n_e = 0.76 \times 10^{18} \text{ cm}^{-3}$ compared with the profile measured in Ref. [Doria et al. (2006)] at $n_e = 0.43 \times 10^{18} \text{ cm}^{-3}$, $T = 3.31 \text{ eV}$, and $d = 2.02 \text{ mm}$.

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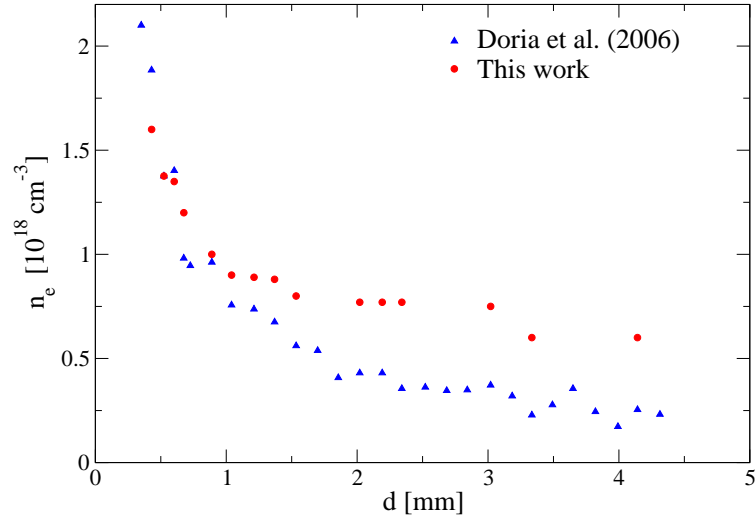


Figure 9: The free electron density distribution of Li II versus normal distance from the sample surface d . Comparison is made with the estimation values in Ref. [Doria et al. (2006)] at 60 ns delay time.

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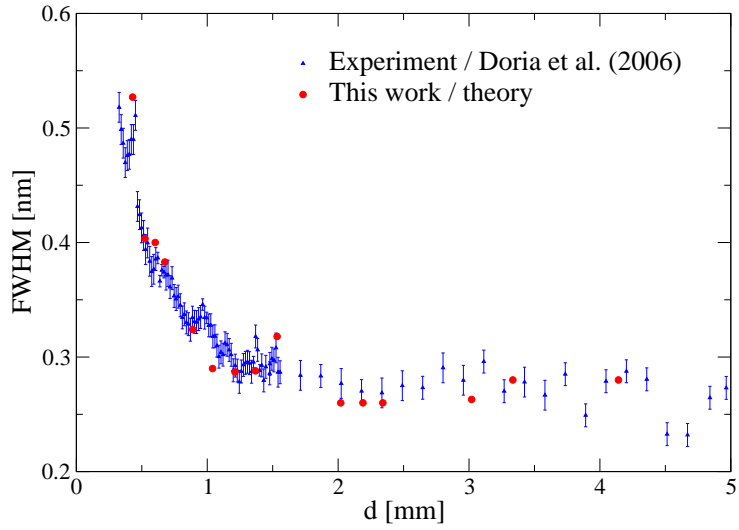


Figure 10: The FWHM of Li II ($2p^3P_{2,1,0} - 2s^3S_1$) 548 nm line versus distance. Comparison is made with the estimated values from measured profiles after 60 ns laser exposure [Doria et al. (2006)].

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Transition		σ^2	σ^2 ⁽¹⁾	f_{if}	f_{if} ⁽¹⁾	f_{if} ⁽²⁾
³ S- ³ P ⁰	2s-2p	1.85014	1.894	0.307485	0.323	0.30665/0.307940
	-3p	0.240332	0.2361	0.182895	0.179	0.18330/0.1871
	-4p	0.0627511	0.0578	0.0605617	-	0.05637/0.0575
	3s-2p	0.210062	0.2201	0.115857	-	0.11416/0.11710
	-3p	11.8357	11.93	0.512237	-	0.51167/0.5128
	-4p	0.7274	0.7274	0.179942	-	0.18583/0.18686
	4s-2p	0.0270884	0.0280	0.0211708	-	0.020787/0.02147
	-3p	1.36309	1.413	0.254529	-	0.25376/0.2550
	-4p	40.69	40.69	0.706735	-	0.70298/0.7036

Table 1: Comparison is given between our calculated values of the radial part of transition matrix-element σ^2 and the oscillator strength of transition f_{if} for triplet transition of Li II and those in Refs. ⁽¹⁾[Cohen and Kelly (1967)] and ⁽²⁾[Theodosiou (1985)].