

# Analytical investigation of electrons capture time effect on the threshold current density reduction in QD spin-lasers

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## Abstract

One of the mechanisms for threshold current density reduction is using spin-polarized carriers generated by electrical spin injection. Electrical spin injection is spin-polarized carrier injection by using a magnetic contact. In this paper, we have solved numerically the rate equations governing on the *InAs* / *GaAs* semiconductor spin with un-polarized and polarized laser field based on quantum dot active region in which *MnAs* / *Al<sub>0.1</sub>Ga<sub>0.9</sub>As* Schottky tunnel barrier treats as the spin injector. For the first time, we demonstrate simultaneously the effects of electrons capture time, and injected current polarization on threshold current density reduction and normalized spin-filtering interval. According to our results, the threshold current density reduction and normalized spin-filtering interval increases by simultaneously with electrons capture time reduction and increase of injected current polarization. The maximum obtained threshold current density reduction and normalized spin-filtering interval values are 0.353 and 0.90, respectively. Finally, we also calculate the spin-up optical gain and from this, we obtain the conditions for achieving optimum optical gain. The maximum obtained spin-up optical gain value is 17.70.

## Keywords

Spin laser- Gain- Threshold Current – Quantum Dot –Filtering

## 1. Introduction

The importance of lasers generally reflects to their practical applications [1-5]. Semiconductor lasers are important due to their widespread applications [3]. Semiconductor lasers use semiconductors as active medium [4]. An active material is pumped to create population inversion and light can be amplified through stimulated emission [3-4]. By the introduction of spin-polarized carriers which is the physical mechanisms that enhance stimulated emission [3], the current density threshold in semiconductor lasers can be reduced [6-13]. Such semiconductor lasers are called semiconductor spin polarized-lasers (SSPLs) [14-16]. Most of the SSPLs are vertical cavity surface emitting lasers (VCSELs) with an active region consisting of III-V Quantum Dots (QDs). The VCSELs are types of semiconductor lasers with perpendicular laser beam emission. A VCSEL should have a resonant cavity with two distributed Bragg reflectors (DBRs). A DBR is a light reflecting device based on Bragg reflections in a periodic structure, alternating high and low refractive indices and with quarter-wave length thick material. It must be highly optically reflective and electrically conductive. Advantages of such laser are low power consumption, low threshold currents and generates less heat, but it also has a lower output power than other semiconductor lasers [10-11]. In this paper, we intend to investigate simultaneously the effects of electrons capture time and

injected current polarization on threshold current density reduction (TCDR) and normalized spin-filtering interval (NSFI) of a QD SSPL by its numerical rate equation solution. For achieving To achieve this aim, we introduce spin polarized injection and present proper materials for to implement that this (section 2). In section 3 have been represented numerically, the solution of rate equations governing on the *InAs* / *GaAs* QDs semiconductor spin with un-polarized and polarized laser field based spin polarized and un-polarized semiconductor laser by considering quadratic spontaneous radiative recombination [12]. As the creation of NSFI and TCDR are two important consequences of spin polarized injection, we compute the effects of injected electron current polarization and electrons capture time on NSFI and TCDR by spotting quadratic spontaneous radiative recombination in section 4 and 5, respectively. In section 6, we calculate spin-up optical gain and from this, we obtain the conditions for achieving optimum optical gain. Finally, we present conclusion and discussion in section 7.

## 2. Suitable Materials for Spin-polarized Injection

Spin-polarized electron injection into semiconductors has been a field of growing interest during the last years [17]. As Since we need electron injection for electronic devices, spintronics devices require spin-polarized

electron injection. A spin-polarization of the current is expected from the different conductivities resulting from the different densities of states for spin-up and spin-down electrons in the ferromagnetic materials. A comfortable way to create of creating spin-polarized electron injection is by passing electron current form through ferromagnetic materials. Spin injectors are materials which create spin-polarized electron injection [4]. There have been many choices for spin injectors but the most obvious choice are is ferromagnetic materials due to their high Curie temperatures, low coercivities and fast switching times [11-15]. The main problem for using ferromagnetic materials is conductivity mismatch, which occurs at the interface between ferromagnetic, and semiconductor materials [18]. There are three solutions to solve for this problem. The first solution is to use a half metallic ferromagnetisms [19] which are materials that possess a band-gap at the Fermi level for one of the spin sub-bands, generally the minority-spin sub-band, making them 100% spin-polarized [19]. The second solution is to use diluted magnetic semiconductors, which have similar conductivity with magnetic materials. Note that Curie temperature of these materials is still well below room temperature. Another solution is to use either an extrinsic or intrinsic tunnel barrier [18]. The advantage of using a tunnel barrier is that it allows ferromagnetic materials to be used as the source of spin-polarized electrons [15]. An intrinsic Schottky barrier is formed when a ferromagnetic material is placed in contact with a semiconductor. It overcomes limitations of the conductivity mismatch without the need for the deposition of a tunnel barrier [15].

### 3. Rate Equations

The electronic transitions shown in Fig. 1, take place between conduction and valence band carriers in QD-SSPLs [20].

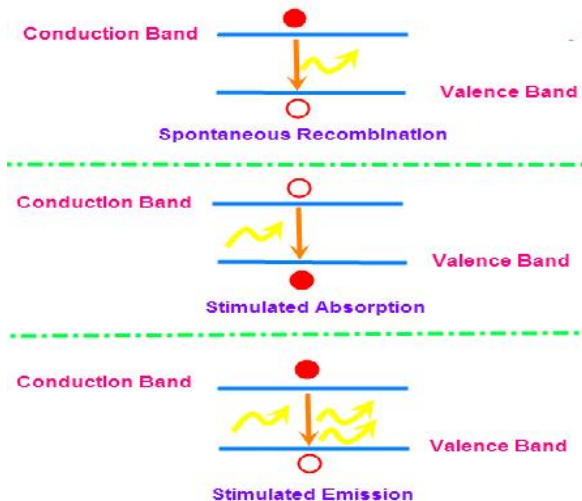


Fig.1. The electronic transitions in a semiconductor material [20].  
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The first of the processes is spontaneous recombination of an electron in the conduction band and a hole in the valence band, which results in incoherent emission. The second process is the photon absorption by the active

material, which promotes the generation of an electron-hole pair and increases the carrier density in both the conduction band and valence band. The third transition is the emission of a photon by means of an electron-hole recombination after the stimulus of another photon already present in the cavity. This process provides optical gain because it starts with one photon and ends with two photons. The dynamics of carrier and photon densities in semiconductor lasers are governed by the coupled rate equations. The rate equations describe how electrons and holes turn into photons. For simplicity, let us assume assuming a constant current injection rate i.e. at each unit time amount of electron is injected into the laser active region. This pumping process as a photon absorption process in the semiconductor material increases the number of electrons in the conduction band and holes in the valence band while the Photon-emitting processes reduce this number of electrons. (This pumping process increases the number of electrons in the conduction band and holes in the valence band. Photon absorption in the semiconductor material increases the number of electrons in the conduction band and holes in the valence band. Photon-emitting processes reduce the number of electrons in the conduction band and holes in the valence band.) The photon-emitting processes are those which generate photons through spontaneous recombination and stimulated emission. Stimulated emitted photons and the spontaneous recombination processes will contribute to increase the photon density, because these processes are producing light inside the device, whereas the photons involved in the stimulated absorption processes cause the opposite effect, thus decreasing the photon number in a time interval. Besides the stimulated absorption, also the material optical loss will also reduce the photon density and expresses how many photons are lost as they propagate at each centimeter of the cavity and as they impinge on the cavity end mirrors.

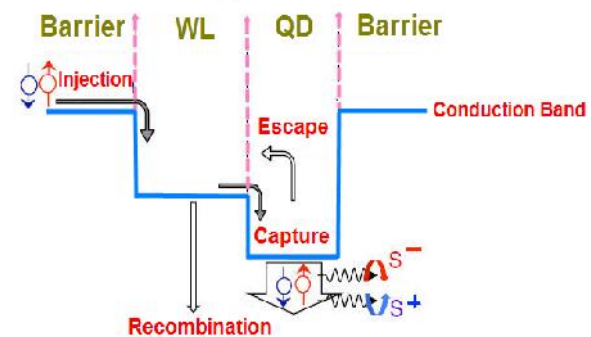


Fig.2. characteristic processes in QD SSPL [21]. (created space between figure caption and the following text)

The QD (Quantum Dot) confine carriers from wetting layer (WL) which acts as a source of carriers. The presence of the WL will affect the dynamical behavior of the device. In QD semiconductor lasers, WL are inevitably present, because of the self-assembly growth process. QD semiconductor lasers will require lower levels of current injection to reach threshold and to keep operating, and the threshold current will be ideally

temperature-insensitive. Each electron of the current is directly injected into the WL and become confined in the WL for a given time, after which it will relax into QD. Besides the possibility to relax into QD, an electron in the WL can either spontaneously recombine with a hole of the valence band or undergo a stimulated emission process, generating a photon of energy “ $h\nu$ ” equal to the energy of the incident photon. The electrons, which get out of the QD don't contribute to the lasing. For the electrons which relaxation into QD, the escape from QD implies a confinement in the WL. By assumption of neutrality of charge, rate equation of QD semiconductor lasers in terms of levels occupancy probability by electrons in QDs and WL ( $f_w, f_{qn}$ ); (the authors have to used the same editor to types the equations) and photon ( $f_s$ ) occupancies is written as[21, 22]

$$\frac{df_w}{dt} = J(1-f_w) - \frac{f_w(1-f_{qn})}{\tau_c} + \frac{2f_{qn}(1-f_w)}{k\tau_e} \quad (1)$$

$$\frac{df_{qn}}{dt} = \frac{kf_w(1-f_{qn})}{2\tau_c} - \frac{f_{qn}(1-f_w)}{\tau_e} - b_q f_{qn}^2 - g(2f_{qn}-1)f_s \quad (2)$$

$$\frac{df_s}{dt} = g(2f_{qn}-1)f_s - \frac{f_s}{\tau_{ph}} \quad (3)$$

where  $J$ ,  $\tau_c$ ,  $\tau_e$ ,  $k$ ,  $b_q$ ,  $\tau_{ph}$  and  $g$  are number of electrons injected into the laser per WL state and unit time, electron capture time, electron escape time, rate of states number in the WL to numbers of QDs, recombination rate in QD, photon lifetime and stimulated emission rate, respectively. Note that spontaneous emission factor and optical confinement factor in equation (3) is 0 and 1, respectively. We neglect spontaneous radiative recombination in equation (1). For the sake of simplicity, we assume a constant current injection rate. This means that at each unit time a very precise amount of electron is injected into the laser active region (this is called the pumping process). (increases the number of electrons in the conduction band and number of holes in the valence band in the device). the results obtained respectively in equations (....) and (...) are the essential of our investigations (the time dependency of levels occupancies probability by electrons in WL and QDs at fixed injection). Following the numerical representations in Figs.3 and 4, respectively we find that these results approach the experimental data of reference [22]. , we investigate time dependency of levels occupancies probability by electrons in WL and QDs at fixed injection in Figs.3 and 4, respectively.

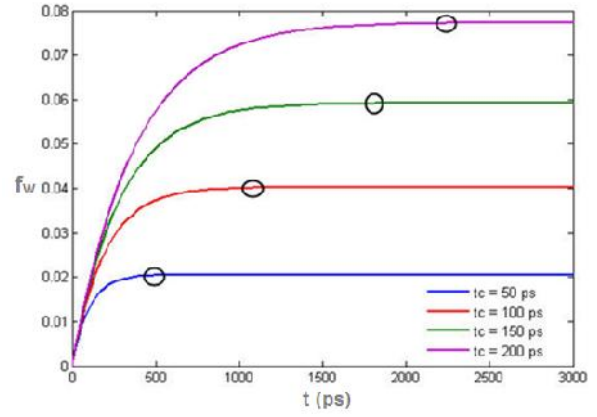


Fig.3. Time dependency of WL levels occupancies probability by electrons of a QD semiconductor laser

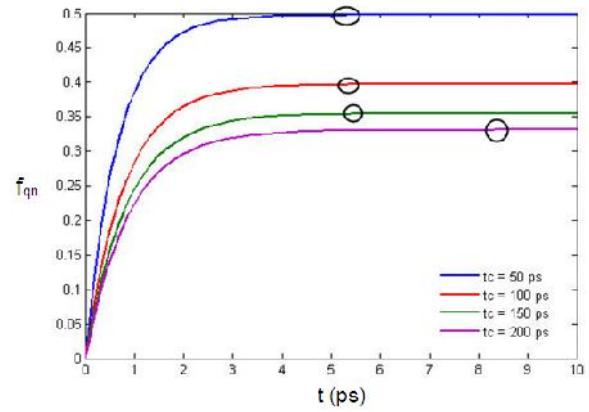


Fig.4. Time dependency of QD levels occupancies probability by electrons of a QD semiconductor laser.

According to these Figs, levels occupancy probabilities by electrons in WL increases with increase in electron capture time by electron capture time grow up while level occupancy probabilities by electrons in QD increases with decreases in electron capture time by electron capture time reduction at the fixed injection. As electrons are directly injected to WL, whatever when electrons capture time is shorter, electrons confined in the QDs faster and levels occupancy probabilities by electrons increases in QD. As shown in Figs. 3 and 4, from points that are characterized with black circle, levels occupancy probability by electrons in QDs and WL have constant trend and saturation is reached. Table 1 and 2 illustrates obtained values of levels occupancy probabilities by electrons in QDs and WL for three various electrons capture time. (make space)

Table 1: Obtained values of electron occupancies in WL for three various electron capture times

$\tau_c = 50 ps$		$\tau_c = 100 ps$		$\tau_c = 150 ps$	
$f_w$	$t (ps)$	$f_w$	$t (ps)$	$f_w$	$t (ps)$
0.0125	91.7065	0.0207	137.8592	0.0418	344.1086
0.0197	308.7805	0.0389	638.1196	0.0564	850.4725
0.0205	527.0261	0.0402	1155.8	0.0592	1814.9

Table 2: Obtained values of levels occupancy probability by electrons in QDs for three various electron capture times

$\tau_c = 50 ps$		$\tau_c = 100 ps$		$\tau_c = 150 ps$	
$f_{qn}$	$t (ps)$	$f_{qn}$	$t (ps)$	$f_{qn}$	$t (ps)$

0.1346	0.2093	0.1297	0.3139	0.1268	0.3767
0.4928	3.1134	0.3943	3.8449	0.3520	4.1493
0.4972	5.3287	0.3970	5.3449	0.3542	5.6493

Fig.5 shows time dependency of photon occupancies. According to this Fig, photon occupancies increase by growing-up increase of levels occupancy probabilities by electrons in QD at the fixed injection. When level occupancy probabilities by electrons increases in QD, the numbers of electrons, which participate in lasing operation increase. Thus, gain increase refers to which describes more coupling of the carriers and light. Therefore, this situation gives rise to stimulated emission and lasing operation is improved.

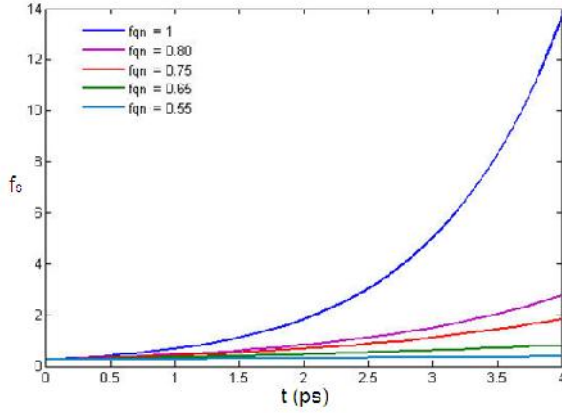


Fig.5. Time dependency of photon levels occupancies of a QD semiconductor laser.

Table 3 demonstrates obtained values for photon occupancies for three various levels occupancy probabilities by electrons in Quantum Dot (QD).

Table 3: Obtained values of photon occupancies for three various levels occupancies probability by electrons in Quantum Dot (QD).

$f_{qn} = 0.70$		$f_{qn} = 0.73$		$f_{qn} = 0.75$	
$f_s$	$t (ps)$	$f_s$	$t (ps)$	$f_s$	$t (ps)$
0.1568	2.2500	0.2377	2.2788	0.3869	2.7059
0.2858	5.2500	0.7433	5.2788	1.5283	5.4534
0.6360	9.2500	3.3986	9.2788	11.4725	9.4845

Now, we generalize rate equation for levels occupancy probabilities by spin-polarized electrons in QD and WL ( $f_{w\pm}, f_{qn\pm}$ ) and photon spin-dependent occupancies ( $f_{s\mp}$ ) related to QDSSPL. Thus, mathematical forms of these rate equations are [21, 22]

$$\frac{df_{w\pm}}{dt} = J_{n\pm}(1-f_{w\pm}) - \frac{f_{w\pm}(1-f_{qn\pm})}{\tau_c} \quad (4)$$

$$+ \frac{2f_{qn\pm}(1-f_{w\pm})}{k\tau_e} \mp \frac{(f_{w+}-f_{w-})}{\tau_{snw}} \quad (5)$$

$$\frac{df_{qn\pm}}{dt} = \frac{kf_{w\pm}(1-f_{qn\pm})}{2\tau_c} - \frac{f_{qn\pm}(1-f_{w\pm})}{\tau_e} - b_q f_{qn\pm}^2$$

$$- g(2f_{qn\pm} + f_{qp\pm} - 1)f_{s\mp} \mp \frac{(f_{qn+} - f_{qn-})}{\tau_{snq}} \quad (6)$$

$$\frac{df_{s\mp}}{dt} = \Gamma_{QD} g(f_{qn\pm} + f_{qp\pm} - 1)f_{s\mp} - \frac{f_{s\mp}}{\tau_{ph}}$$

Where  $J_{n\pm}$  is number of spin-polarized electrons injected into the laser per WL state and unit time.  $\tau_{snw}$  and  $\tau_{snq}$  are spin relaxation time in WL and QD which limit to infinite. We neglect spin-dependent spontaneous radiative recombination in WL. Note that due to charge neutrality, we could decouple the rate equations for spin-dependent electrons from those for holes. Figs. 6 and 7 determine time dependency of levels occupancy probabilities by spin-up electrons in QD and WL at the fixed spin polarized injection.

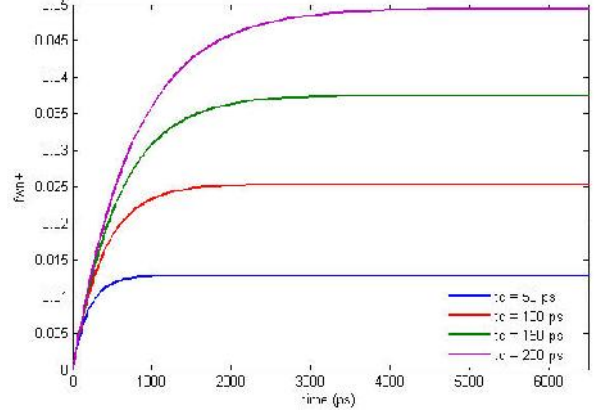


Fig.6. Time dependency of WL levels occupancies probability by spin-up electrons for a QD SSPL.

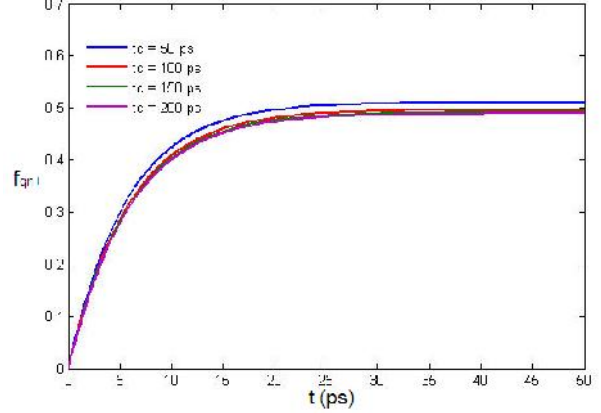


Fig.7. Time dependency of QD levels occupancies probability by spin-up electrons for a QDSSPL.

These figures imply that levels occupancy probabilities by spin-up electrons in WL increases by electron capture time grow up increase while levels occupancy probabilities by spin-up electrons in QD increases by electron capture time reduction at the fixed spin polarized injection. As spin polarized electrons are directly injected to WL, whatever when electrons capture time is shorter, spin-up electrons confined in the QDs faster and levels occupancy probabilities by spin-up electrons increases in QD. Finally, as shown in Figs. 6 and 7, finally levels occupancy probability by spin-up electrons in QDs and WL have constant trend and saturation is reached. Table 4 and 5 illustrates obtained values of levels occupancy probabilities by spin-up electrons in QDs and WL for three various electrons capture times.



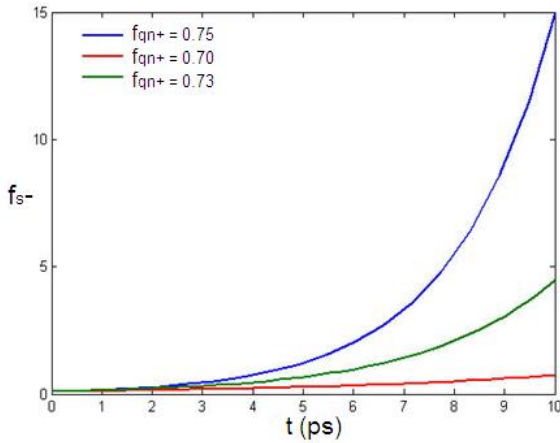
**Table 4: Obtained values of levels occupancies probability by spin-up electrons in WL for three various of electron capture time.**

$\tau_c = 50ps$		$\tau_c = 100ps$		$\tau_c = 150ps$	
$f_{w+}$	$t(ps)$	$f_{w+}$	$t(ps)$	$f_{w+}$	$t(ps)$
0.0096	270.3789	0.0164	407.3349	0.0226	530.2278
0.0111	390.3743	0.0203	626.3705	0.0288	844.1998
0.0128	1009.3	0.0253	2333.1	0.0375	3688.1

**Table 5: Obtained values of levels occupancies probability by spin-up electrons in QD for three various of electron capture time.**

$\tau_c = 50ps$		$\tau_c = 100ps$		$\tau_c = 150ps$	
$f_{qn+}$	$t(ps)$	$f_{qn+}$	$t(ps)$	$f_{qn+}$	$t(ps)$
0.3500	6.4821	0.3425	6.7467	0.2736	4.7492
0.4964	19.7447	0.4823	20.1163	0.4739	18.9973
0.5099	33.4947	0.4959	33.8663	0.4917	37.7473

Fig. 8 shows time dependency of negative helicity (NH) photon occupancies at the fixed spin polarized injection. According to this Fig, NH photon occupancies increases by growing-up of with increase in levels occupancy probabilities by spin-up electrons in QD at the fixed spin-polarized injection. When levels-occupancy probabilities by spin-up electrons increases in QD, numbers of spin-up electrons which participate in lasing operation increase grow-up. Thus, gain increase refers to which-describes more coupling of the carriers and light. Therefore, this situation give rise to stimulated emission and lasing operation is improved.



**Fig.8. Time dependency of NH photon occupancies for a QDSSPL.**

Table 6 demonstrates shows obtained values for NH photon occupancies for three various levels occupancy probabilities by spin-up electrons in QD.

**Table 6: Obtained values of NH photon occupancies for three various levels occupancies probability by spin-up electrons in QD**

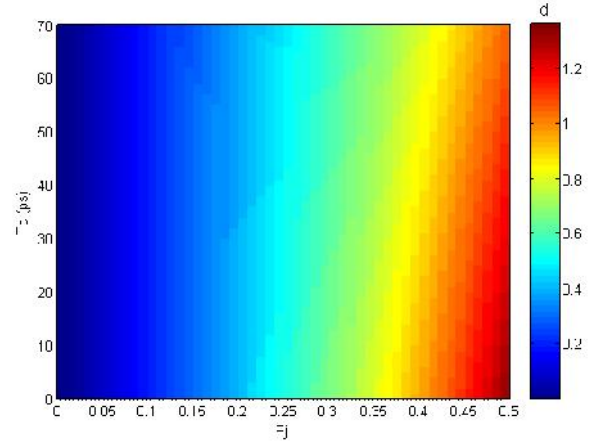
$f_{qn+} = 0.70$		$f_{qn+} = 0.73$		$f_{qn+} = 0.75$	
$f_{s-}$	$t(ps)$	$f_{s-}$	$t(ps)$	$f_{s-}$	$t(ps)$
0.1051	0.2500	0.1105	0.2644	0.1163	0.3014
0.1568	2.2500	0.2377	2.2788	0.3869	2.7059
0.2858	5.2500	0.7433	5.2788	1.5283	5.4534

#### 4. NSFI width

Creation of NSFI is one of the important consequences of spin polarized injection. The width of this interval can be obtained analytically from rate equations (4)-(6) which can be presented as [21, 22]

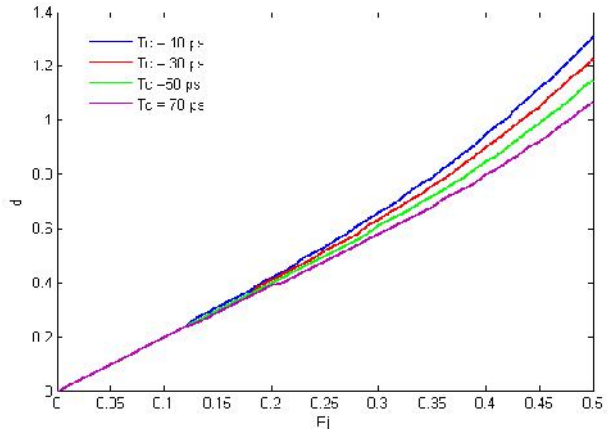
$$d = \left[ \frac{1}{(1-|P_{Jn}|)} \right] - \left[ \frac{4}{(2+|P_{Jn}|)^2} \times \left[ 1 + \frac{18|P_{Jn}|^3 b_q \tau_c}{1+6|P_{Jn}|+3|P_{Jn}|^2-10|P_{Jn}|^3} \right] \right] \quad (7)$$

Where  $|P_{Jn}|$  is the polarization of injected electron current. Fig.9 shows NSFI versus simultaneously variations of polarization of injected electron current and electron capture time.



**Fig.9. NSFI versus variations of polarization of injected electron current and electron capture time.**

In Fig.9 dark, red and blue areas demonstrate highest and lowest NSFI, respectively. According to it, we find out that NSFI increases with simultaneously electron capture time reduction and increase of injected electron current polarization. Increase of NSFI leads to power consumption reduction of lasers and enhances laser dynamic performance. This advantage is obtained by using electrical spin injection in QD/QW SSPLs. Fig. 8 presents NSFI versus variations of injected electron current polarization for four various electrons capture times.



**Fig.10. NSFI versus variations of injected electron current polarization for four various electron capture times.**

Fig.10 shows that NSFI increases by with injected electron current polarization grow-up increase per specific electron capture time. When electron capture time grows up increase, it takes a longer time that for electrons to fall into QD. Thus, we observe smaller levels occupancy probabilities by spin-up electrons in QD and therefore NSFI reduction. Note that up to  $|P_J| = 0.12$ , NSFI is equal per all of electrons capture times. Table 7 illustrates obtained values for NSFI for three various polarizations of injected electron current at different periods of times.

**Table 7: Obtained values of NSFI for three various polarizations of injected electron current at different period of times.**

$ P_{Jn}  = 0.2$		$ P_{Jn}  = 0.3$		$ P_{Jn}  = 0.4$	
$d$	$t_c(ps)$	$d$	$t_c(ps)$	$d$	$t_c(ps)$
0.41	30	0.63	30	0.90	30
0.40	50	0.61	50	0.85	50
0.39	70	0.58	70	0.80	70

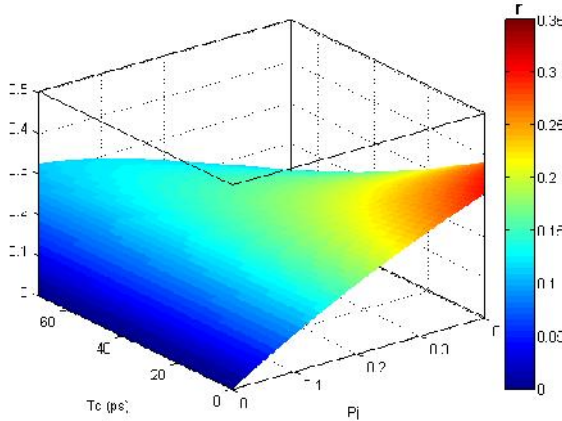
Based on Table 7 and obtained values, NSFI maximum is 0.90. Our obtained result in Table 7 (rephrase this as: from the values obtained in Table 7, we find that the NSFI maximum value is 0.90.)

## 5. TCDR

One of the spin polarized injection benefits is TCDR which results from the creation of NSFI [23-25]. In this interval, only charge carriers with majority spin species contribute at during lasing process. TCDR can be obtained analytically from rate equations (4)-(6) given (presented) by the following equation [21, 22]:

$$r = 1 - \frac{4}{(2 + |P_{Jn}|)^2} \times \left[ 1 + \frac{18|P_{Jn}^3|b_q\tau_c}{1 + 6|P_{Jn}| + 3|P_{Jn}^2| - 10|P_{Jn}^3|} \right] \quad (8)$$

Fig.11 shows TCDR versus simultaneously variations of polarization of injected electron current and electron capture time.



**Fig.11. TCDR versus variations of polarization of injected electron current and electron capture time.**

According to figure 11, we find out that TCDR increases with simultaneously electron capture time reduction and increase in injected electron current polarization. Also, increase of TCDR leads to power consumption reduction of lasers and enhances laser dynamic performance. Such a reduction is obtained by using electrical spin injection

in QW SSPLs. Increase of electrical spin injection leads to increase in polarization of injected electron current and laser bandwidth. Note that TCDR increases by as injected electron current polarization grow-up increases per specific electron capture time. When electron capture time grows up increases, we observe smaller NSFI and TCDR. Table 8 illustrates obtained values for TCDR for three various polarizations of injected electron current at different period of times.

**Table 8: Obtained values of TCDR for three various polarizations of injected electron current at different period of times.**

$ P_{Jn}  = 0.1$		$ P_{Jn}  = 0.2$		$ P_{Jn}  = 0.4$	
$r$	$t_c(ps)$	$r$	$t_c(ps)$	$r$	$t_c(ps)$
0.089	30	0.174	30	0.353	30
0.087	50	0.168	50	0.341	50
0.085	70	0.163	70	0.328	70

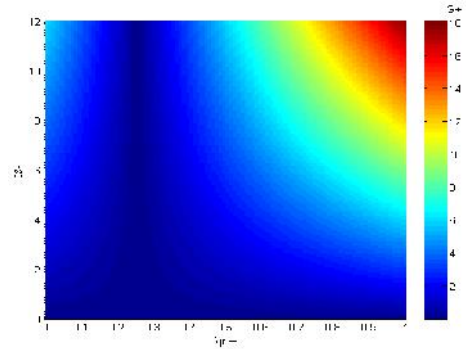
Based on Table 8 and The values obtained in Table 8 shows the TCDR maximum at 0.353.

## 6. Optical gain

The optical gain describes coupling of the carriers and light, which gives rise to stimulated emission [22, 26]. According to the importance of this quantity, we intend to investigate variation of spin-dependent optical gain versus levels occupancy probabilities by spin-up electrons in QD and NH photon occupancies. Spin-dependent gain term can be written as [21, 22]

$$G_{\pm} = g(f_{qn\pm} + f_{qp\pm} - 1)f_{s\mp} \quad (9)$$

Fig. 12 shows that spin-up gain term increases with by simultaneously rising of levels occupancies probability by spin-up electrons in QD and NH photon occupancies.



**Fig.12. Spin-up optical gain versus variations of levels occupancies probability by spin-up electrons in QD and NH photon occupancies**

High levels occupancy probabilities by spin-up electrons in QD lead to high NH photon occupancies, then we obtain higher spin-up optical gain values. Increase of spin-up optical gain ensures efficiency of laser. Table 9 demonstrates presents obtained values for spin-up optical gain for four various levels occupancies probability by spin-up electrons in QD.

**Table 9: Obtained values of spin-up optical gain for four various levels occupancy probabilities by electrons in Quantum Dots (QDs).**

$f_{qn+} = 1$		$f_{qn+} = 0.80$		$f_{qn+} = 0.75$		$f_{qn+} = 0.55$	
$f_{s-}$	$G_+$	$f_{s-}$	$G_+$	$f_{s-}$	$G_+$	$f_{s-}$	$G_+$
3.5	5.40	3.5	3.96	3.5	3.60	3.5	2.16
8.2	12.45	8.2	9.13	8.2	8.30	8.2	4.98
11.7	17.70	11.7	12.98	11.7	11.80	11.7	7.08

Based on Table 9 and obtained values, spin-up optical gain maximum is 17.70, respectively. The values obtained in Table 9 show that the spin-up optical gain maximum is obtained at 17.70.

## 7. Conclusion

According to the above discussion, it appearances there appears an intensive dependency of QD SSPL operations on spin injection and longer spin relaxation time. Using numerical rate equations, we demonstrate for the first time, the simultaneously effect of electron capture time and injected current polarization on TCDR and NSFI. It is then found that, the TCDR and NSFI increases by simultaneously electron capture time reduction and increase of injected current polarization. This increase in TCDR and NSFI leads to lower power consumption and enhances the lasers dynamic performance. The maximum values obtained for TCDR and NSFI are 0.353 and 0.90, respectively. Spin-up optical gain term increases by with simultaneously rise of levels occupancy probabilities by spin-up electrons in QD and NH photon occupancies. The maximum obtained Spin-up optical gain is 17.70. These results show that laser is a very promising candidate as emerging field based on colloidal semiconductor QDs typically II–VI, such as CdS, CdSe, ZnSe, and ZnTe [27, 28,29]. By providing practical paths to new spin-based devices, we expect that studies of spin-lasers will also offer motivation to understanding of spin transport and magnetism.

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