Analytical investigation of electrons capture time effect on the threshold current density reduction in QD spin-lasers

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Abstract

One of the mechanisms for threshold current density reduction is using spin polarized carriers generated by electrical spin injection. Electrical spin injection is spin-polarized carrier injection by using a magnetic contact. In this paper, we have solved numerically rate equations governing on semiconductor spin un-polarized and polarized laser with InAs/GaAs based quantum dot active region in which $MnAs/Al_{0.1}Ga_{0.9}As$ Schottky tunnel barrier treat as the spin injector. For the first time, we demonstrate simultaneously effect of electrons capture time and injected current polarization on threshold current density reduction and normalized spin-filtering interval. According to our result threshold current density reduction and normalized spin-filtering interval increases by simultaneously electrons capture time reduction and increasing of injected current polarization. Maximum obtained threshold current density reduction and normalized spin-filtering interval values are 0.353 and 0.90, respectively. Finally we calculate spin-up optical gain and from this we obtained the conditions for achieving optimum optical gain. Maximum obtained spin-up optical gain value is 17.70.

Keywords

Spin laser- Gain- Threshold Current – Quantum Dot – Filtering

1. Introduction

The importance of lasers generally reflects to their practical applications [1-5]. Semiconductor lasers are important due to its wide spread applications [3]. Semiconductor lasers use semiconductor as active medium [4]. An active material is pumped to create population inversion and light can be amplified through stimulated emission [3-4]. By introduction of spinpolarized carriers which is physical mechanisms that enhance stimulated emission,[3] we can reduce current density threshold in semiconductor lasers [6-13]. Such semiconductor lasers are called semiconductor spin polarized-lasers (SSPLs) [14-16]. Most of the SSPLs are vertical cavity surface emitting lasers (VCSELs) with active region consisting of III-V Quantum Dots (QDs). The VCSELs are type of semiconductor lasers with laser beam emission perpendicular. A VCSEL should have a resonant cavity with two distributed Brag reflectors (DBRs). A DBR is light reflecting device based on Brag reflections in a periodic structure, alternating high and low refractive indices and with quarter-wave length material thick. It must be highly optically reflective and electrically conductive. Advantages of such laser are low power consumption, low threshold currents and generate less heat, but it also have lower output power than other semiconductor lasers [10-11]. In this paper, we intend to investigate simultaneously effects of electrons capture time and injected current polarization on threshold current density reduction (TCDR) and normalized spinfiltering interval (NSFI) of a QD SSPL by its numerical rate equation solution. For achieving this aim, we introduce spin polarized injection and present proper materials for implement that (section 2). In section 3 have been represented numerically solution of rate equations governing on InAs/GaAs QDs based spin polarized and un-polarized semiconductor laser by considering quadratic spontaneous radiative recombination [12]. As creation of NSFI and TCDR are two important consequences of spin polarized injection, we compute the effects of injected electron current polarization and electrons capture time on NSFI and TCDR by spotting quadratic spontaneous radiative recombination in section 4 and 5, respectively. In section 6, we calculate spin-up optical gain and from this we obtain the conditions for achieving optimum optical gain. Finally, we present conclusion and discussion in section 7.

2. Suitable Materials for Spin-polarized Injection

Spin-polarized electron injection into semiconductors has been a field of growing interest during the last years [17]. As we need electron injection for electronic devices, spintronics devices require spin-polarized electron injection. A spin-polarization of the current is expected from the different conductivities resulting from the different densities of states for spin-up and spin-down electrons in the ferromagnetic materials. Comfortable way to create spin-polarized electron injection is passing electron current form ferromagnetic materials. Spin injectors are materials which create spin-polarized electron injection [4]. There have been many choices for spin injectors but the most obvious choice are ferromagnetic materials due to their high Curie temperatures, low coercivities and fast switching times [11-15]. The main problem for using ferromagnetic materials is conductivity mismatch which occurs at the interface between ferromagnetic and semiconductor materials [18]. There are three solutions to solve this problem. The first solution is to use a half metallic ferromagnetism [19] which are materials that possess a band-gap at the Fermi level for one of the spin subbands, generally the minority-spin sub-band, making them 100% spin-polarized [19]. The second solution is to use dilute magnetic semiconductors which have similar conductivity with magnetic materials. Note that Curie temperature of these materials is still well below room temperature. Another solution is to use either an extrinsic or intrinsic tunnel barrier. [18] The advantage of using a tunnel barrier is that it allows ferromagnetic materials to be used as the source of electrons [15]. An intrinsic Schottky spin-polarized barrier is formed when a ferromagnetic material is placed in contact with a semiconductor. It overcomes limitations of the conductivity mismatch without the need for the deposition of a tunnel barrier [15].

3. Rate Equations

The electronic transitions which show in Fig.1, take place between conduction and valence band carriers in QD-SSPLs [20].





conduction band and valence band. The third transition is

the emission of a photon by means of an electron-hole recombination after the stimulus of another photon already present in the cavity. This process provides optical gain because it starts with one photon and ends with two photons. The dynamics of carrier and photon densities in semiconductor lasers are governed by the coupled rate equations. Rate equations describe how electrons and holes turn into photons. For simplicity, let us assuming a constant current injection rate i.e. at each unit time amount of electron is injected into the laser active region. This pumping process increases the number of electrons in the conduction band and holes in the valence band. Photon absorption in the semiconductor material increases the number of electrons in the conduction band and holes in the valence band. The number of electrons in the conduction band and holes in the valence band is reduced by photon-emitting processes. The photon-emitting processes are those which generate photons through spontaneous recombination and stimulated emission. Stimulated emitted photons and the spontaneous recombination processes will contribute to increase the photon density, because these processes are producing light inside the device, whereas the photons involved in the stimulated absorption processes cause the opposite effect, thus decreasing the photon number in a time interval. Besides the stimulated absorption, also the material optical loss will reduce the photon density and expresses how many photons are lost as they propagate at each centimeter of the cavity and as they impinge on the cavity end mirrors.





The QD (Quantum Dot) confine carriers from wetting layer (WL) which acts as a source of carriers. Presence of the WL will affect the dynamical behavior of the device. In QD semiconductor lasers, WL are inevitably present, consequence of the self-assembly growth process. QD semiconductor lasers will require lower levels of current injection to reach threshold and to keep operating, and the threshold current will be ideally temperature-insensitive. Each electron of the current is directly injected into the WL and become confined in the WL for a time, after which it will relax into OD. Besides the possibility to relax into QD, an electron in the WL can either spontaneously recombine with a hole of the valence band or undergo a stimulated emission process, generating a photon of energy hu equal to the energy of the incident photon. The electrons which get out of the QD don't contribute to the lasing. For the electrons which relax into QD. The escape from QD implies a confinement in the WL. By assumption of neutrality of charge, rate equation of QD semiconductor lasers in terms of levels occupancy probability by electrons in QDs and WL (f_w, f_{qn}) and photon (f_s) occupancies is written as [21, 22]

$$\frac{df_{w}}{dt} = \overline{J(1-f_{w})} - \frac{f_{w}(1-f_{qn})}{\tau_{c}} + \frac{2f_{qn}(1-f_{w})}{k\tau_{e}}$$
(1)
$$\frac{df_{qn}}{dt} = \frac{kf_{w}(1-f_{qn})}{2\tau_{c}} - \frac{f_{qn}(1-f_{w})}{\tau_{e}} - b_{q}f_{qn}^{2} - g(2f_{qn}-1)f_{s}$$
(2)

$$\frac{df_s}{dt} = g \left(2 \operatorname{f}_{qn} - 1\right) f_s - \frac{f_s}{\tau_{ph}}$$
(3)

Where J, τ_c , τ_e , k, b_q , τ_{ph} and g are number of electrons injected into the laser per WL state and unit time, electron capture time, electron escape time, rate of states number in the WL to numbers of QDs, recombination rate in QD, photon lifetime and stimulated emission rate, respectively. Note that spontaneous emission factor and optical confinement factor in equation (3) is 0 and 1, respectively. We neglect spontaneous radiative recombination in equation (1). For the sake of simplicity, we assume a constant current injection rate. This means that at each unit time a very precise amount of electron is injected into the laser active region. This pumping process increases the number of electrons in the conduction band and number of holes in the valence band in the device. According to experimental data of reference [22], we investigate time dependency of levels occupancies probability by electrons in WL and QDs at fixed injection in Figs.3 and 4, respectively.



Fig.3. Time dependency of WL levels occupancies probability by electrons of a QD semiconductor laser



Fig.4. Time dependency of QD levels occupancies probability by electrons of a QD semiconductor laser.

According to these Figs, levels occupancies probability by electrons in WL increases by electron capture time grow up while levels occupancies probability by electrons in QD increases by electron capture time reduction at the fixed injection. As electrons directly injected to WL, whatever electrons capture time be shorter, electrons confined in the QDs faster and levels occupancy probability by electrons increases in QD. As shown in Figs. 3 and 4, from points which are characterized with black circle, levels occupancy probability by electrons in QDs and WL have constant trend and saturation reaches. Table 1 and 2 illustrates obtained values of levels occupancy probability by electrons in QDs and WL for three various electrons capture time.

 Table 1: Obtained values of electron occupancies in WL for three various electron capture times

$\tau_c = 50 ps$		$\tau_c = 100 ps$		$\tau_c = 150 ps$	
f_w	f_w $t(ps)$ f_w		t(ps)	f_w	t(ps)
0.0125	91.7065	0.0207	137.8592	0.0418	344.1086
0.0197	308.7805	0.0389	638.1196	0.0564	850.4725
0.0205	527.0261	0.0402	1155.8	0.0592	1814.9

 Table 2: Obtained values of levels occupancy probability by

 electrons in QDs for three various electron capture times

$\tau_c = 50 ps$		$\tau_c = 1$	00 <i>ps</i>	$\tau_c = 150 ps$		
f_{qn}	t(ps)	f_{qn}	t(ps)	f_{qn}	t(ps)	
0.1346	0.2093	0.1297	0.3139	0.1268	0.3767	
0.4928	3.1134	0.3943	3.8449	0.3520	4.1493	
0.4972	5.3287	0.3970	5.3449	0.3542	5.6493	

Fig.5 shows time dependency of photon occupancies. According to this Fig, photon occupancies increase by growing up of levels occupancies probability by electrons in QD at the fixed injection. When levels occupancies probability by electrons increases in QD, numbers of electrons which participate in lasing operation grow up. Thus gain increase which describes more coupling of the carriers and light. Therefore, this situation give rise to stimulated emission and lasing operation improve.



Fig.5. Time dependency of photon levels occupancies of a QD semiconductor laser.

Table 3 demonstrates obtained values for photon occupancies for three various levels occupancies probability by electrons in Quantum Dot (QD).

Table 3: Obtained values of photon occupancies for three various levels occupancies probability by electrons in Quantum Dot (QD).

$f_{qn} = 0.70$		$f_{qn} = 0.73$		$f_{qn} = 0.75$	
f_s	t(ps)	f_s	t(ps)	f_s	t(ps)
0.1568	2.2500	0.2377	2.2788	0.3869	2.7059
0.2858	5.2500	0.7433	5.2788	1.5283	5.4534
0.6360	9.2500	3.3986	9.2788	11.4725	9.4845

Now, we generalize rate equation for levels occupancies probability by spin polarized electrons in QD and WL $(f_{w\pm}, f_{qn\pm})$ and photon spin-dependent occupancies $(f_{s\mp})$ related to QDSSPL. Thus, mathematical forms of these rate equations are [21, 22]

$$\frac{df_{w\pm}}{dt} = J_{n\pm}(1 - f_{w\pm}) - \frac{f_{w\pm}(1 - f_{qn\pm})}{\tau_c} + \frac{2f_{qn\pm}(1 - f_{w\pm})}{k\tau_e} \mp \frac{(f_{w\pm} - f_{w-})}{\tau_{snw}} + \frac{df_{qn\pm}}{2\tau} - \frac{kf_{w\pm}(1 - f_{qn\pm})}{2\tau} - \frac{f_{qn\pm}(1 - f_{w\pm})}{\tau_{snw}} - b_q f_{qn\pm}^2 \quad (5)$$

$$\frac{d}{dt} \frac{f_{s_{\mp}}}{f_{gp\pm}} = \Gamma_{QD} g (f_{qn\pm} + f_{qp\pm} - 1) f_{s_{\mp}} + \mp \frac{(f_{qn\pm} - f_{qn-})}{\tau_{snq}}$$

$$\frac{d}{dt} \frac{f_{s_{\mp}}}{f_{s_{\mp}}} = \Gamma_{QD} g (f_{qn\pm} + f_{qp\pm} - 1) f_{s_{\mp}} - \frac{f_{s_{\mp}}}{\tau_{ph}}$$
(6)

Where $J_{n\pm}$ is number of spin-polarized electrons injected into the laser per WL state and unit time. τ_{snw} and τ_{snq} are spin relaxation time in WL and QD which limit to infinite. We neglect spin-dependent spontaneous radiative recombination in WL. Note that due to charge neutrality, we could decouple the rate equations for spin-dependent electrons from those for holes. Figs. 6 and 7 determine time dependency of levels occupancies probability by spin-up electrons in QD and WL at the fixed spin polarized injection.



Fig.6. Time dependency of WL levels occupancies probability by spin-up electrons for a QD SSPL.



Fig.7. Time dependency of QD levels occupancies probability by spin-up electrons for a QD SSPL.

These figures imply that levels occupancies probability by spin-up electrons in WL increases by electron capture time grow up while levels occupancies probability by spin-up electrons in QD increases by electron capture time reduction at the fixed spin polarized injection. As spin polarized electrons directly injected to WL, whatever electrons capture time is shorter, spin-up electrons confined in the QDs faster and levels occupancy probability by spin-up electrons increases in QD. As shown in Figs. 6 and 7, finally levels occupancy probability by spin-up electrons in QDs and WL have constant trend and saturation reaches. Table 4 and 5 illustrates obtained values of levels occupancy probability by spin-up electrons in QDs and WL for three various electrons capture times.

 Table 4: Obtained values of levels occupancies probability by spinup electrons in WL for three various of electron capture time.

$\tau_c = 50 ps$		$\tau_c = 100 ps$		$\tau_c = 150 ps$	
f_{w+}	t(ps)	f_{w+}	t(ps)	f_{w+}	t(ps)
0.0096	270.3789	0.0164	407.3349	0.0226	530.2278
0.0111	390.3743	0.0203	626.3705	0.0288	844.1998
0.0128	1009.3	0.0253	2333.1	0.0375	3688.1

 Table 5: Obtained values of levels occupancies probability by spinup electrons in QD for three various of electron capture time.

$\tau_c = 50 ps$		$\tau_c = 100 ps$		$\tau_c = 150 ps$	
f_{qn+}	t(ps)	f_{qn+}	t(ps)	f_{qn+}	t(ps)

0.3500	6.4821	0.3425	6.7467	0.2736	4.7492
0.4964	19.7447	0.4823	20.1163	0.4739	18.9973
0.5099	33.4947	0.4959	33.8663	0.4917	37.7473

Fig. 8 shows time dependency of negative helicity (NH) photon occupancies at the fixed spin polarized injection. According to this Fig, NH photon occupancies increases by growing up of levels occupancies probability by spinup electrons in QD at the fixed spin-polarized injection. When levels occupancies probability by spin-up electrons increases in QD, numbers of spin-up electrons which participate in lasing operation grow up. Thus gain increase which describes more coupling of the carriers and light. Therefore this situation give rise to stimulated emission and lasing operation improve.



Fig.8. Time dependency of NH photon occupancies for a QD SSPL.

Table 6 demonstrates obtained values for NH photon occupancies for three various levels occupancies probability by spin-up electrons in QD.

Table 6: Obtained values of NH photon occupancies for three various levels occupancies probability by spin-up electrons in QD

$f_{qn+} = 0.70$		f_{qn+} =	= <i>o</i> .73	$f_{qn+} = 0.75$		
f_{s^-}	t(ps)	f_{s^-}	t(ps)	f_{s^-}	t(ps)	
0.1051	0.2500	0.1105	0.2644	0.1163	0.3014	
0.1568	2.2500	0.2377	2.2788	0.3869	2.7059	
0.2858	5.2500	0.7433	5.2788	1.5283	5.4534	

4. NSFI width

Creation of NSFI is one of important consequences of spin polarized injection. Width of this interval can be obtained analytically from rate equations (4)-(6) which can be presented as [21, 22]

$$d = \left[\frac{1}{(1-|P_{j_n}|)}\right] - \left[\frac{4}{(2+|P_{j_n}|)^2} \times \left[1 + \frac{18|P^3_{j_n}|b_q \tau_c}{1+6|P_{j_n}|+3|P^2_{j_n}|-10|P^3_{j_n}|}\right]\right]$$
(7)

Where $|P_{Jn}|$ is polarization of injected electron current. Fig.9 shows NSFI versus simultaneously variations of polarization of injected electron current and electron capture time.



Fig.9. NSFI versus variations of polarization of injected electron current and electron capture time.

In Fig.9 dark red and blue areas demonstrate highest and lowest NSFI, respectively. According to it, we find out that NSFI increases with simultaneously electron capture time reduction and increase injected electron current polarization. Increase of NSFI leads to power consumption reduction of lasers and enhances laser dynamic performance. This advantage is obtained by using electrical spin injection in QD/QW SSPLs. Fig. 8 presents NSFI versus variations of injected electron current polarization for four various electrons capture times.



Fig.10. NSF1 versus variations of injected electron current polarization for four various electron capture times.

Fig.10 shows that NSFI increases by injected electron current polarization grow up per specific electron capture time. When electron capture time grows up, it takes longer time that electrons fall into QD. Thus, we observe smaller levels occupancies probability by spin-up electrons in QD and therefore NSFI reduction. Note that up to $|P_j| = 0.12$, NSFI is equal per all of electrons capture times. Table 7 illustrates obtained values for NSFI for three various polarizations of injected electron current at different times.

 Table 7: Obtained values of NSFI for three various polarizations of injected electron current at different times.

$$|P_{J_n}| = 0.2$$
 $|P_{J_n}| = 0.3$ $|P_{J_n}| = 0.4$

d	$t_c(ps)$	d	$t_c(ps)$	d	$t_c(ps)$
0.41	30	0.63	30	0.90	30
0.40	50	0.61	50	0.85	50
0.39	70	0.58	70	0.80	70

Based on Table 7 and obtained values, NSFI maximum is 0.90. Our obtained result in Table 7

5. TCDR

One of spin polarized injection benefits is TCDR which results from Creation of NSFI [23-25]. In this interval, only charge carrier with majority spin species contribute at lasing process. TCDR can be obtained analytically from rate equations (4)-(6) which can be presented as [21, 22]

$$r = 1 - \frac{4}{\left(2 + \left|P_{J_{n}}\right|\right)^{2}} \times \left[1 + \frac{18\left|P_{J_{n}}^{3}\right| b_{q}\tau_{c}}{1 + 6\left|P_{J_{n}}\right| + 3\left|P_{J_{n}}^{2}\right| - 10\left|P_{J_{n}}^{3}\right|}\right]$$
(8)

Fig. 11 shows TCDR versus simultaneously variations of polarization of injected electron current and electron capture time.



Fig.11. TCDR versus variations of polarization of injected electron current and electron capture time.

According to figure 11, we find out that TCDR increases with simultaneously electron capture time reduction and increase injected electron current polarization. Also, Increase of TCDR leads to power consumption reduction of lasers and enhances laser dynamic performance. Such a reduction is obtained by using electrical spin injection in QW SSPLs. Increase of electrical spin injection leads to raise polarization of injected electron current and laser bandwidth. Note that TCDR increases by injected electron current polarization grow up per specific electron capture time. When electron capture time grows up, we observe smaller NSFI and TCDR. Table 8 illustrates obtained values for TCDR for three various polarizations of injected electron current at different times.

 Table 8: Obtained values of TCDR for three various polarizations of injected electron current at different times.

$\left P_{Jn}\right =0.1$		$\left P_{Jn}\right = 0.2$		$\left P_{Jn}\right =0.4$	
r	$t_c(ps)$	r	$t_c(ps)$	r	$t_c(ps)$
0.089	30	0.174	30	0.353	30
0.087	50	0.168	50	0.341	50
0.085	70	0.163	70	0.328	70

Based on Table 8 and obtained values, TCDR maximum is 0.353.

6. Optical gain

The optical gain describes coupling of the carriers and light, which gives rise to stimulated emission [22, 26]. According to importance of this quantity, we intend to investigate variation of spin-dependent optical gain versus levels occupancies probability by spin-up electrons in QD and NH photon occupancies. Spin-dependent gain term can be written as [21, 22]

$$G_{\pm} = g \left(f_{qn\pm} + f_{qp\pm} - 1 \right) f_{S\mp}$$
(9)

Fig. 12 shows that spin-up gain term increases by simultaneously rising of levels occupancies probability by spin-up electrons in QD and NH photon occupancies.



Fig.12. Spin-up optical gain versus variations of levels occupancies probability by spin-up electrons in QD and NH photon occupancies

High levels occupancies probability by spin-up electrons in QD lead to high NH photon occupancies, then we obtain higher spin-up optical gain values. Increase of spin-up optical gain ensures efficiency of laser. Table 9 demonstrates obtained values for spin-up optical gain for four various levels occupancies probability by spin-up electrons in QD.

Table 9: Obtained values of spin-up optical gain for four various levels occupancy probability by electrons in Quantum Dots(QDs).

$f_{qn+} = 1$		$f_{qn+} = 0.80$		$f_{qn+} = 0.75$		$f_{qn+} = 0.55$	
f_{s^-}	$G_{_+}$	f_{s^-}	$G_{_+}$	f_{s^-}	$G_{_+}$	f_{s^-}	$G_{_+}$
3.5	5.40	3.5	3.96	3.5	3.60	3.5	2.16
8.2	12.45	8.2	9.13	8.2	8.30	8.2	4.98
11.7	17.70	11.7	12.98	11.7	11.80	11.7	7.08

Based on Table 9 and obtained values, spin-up optical gain maximum is 17.70, respectively.

7. Conclusion

According to above discussion, it appearances intensive dependency of QD SSPL operations on spin injection and longer spin relaxation time. Using numerical rate equations, we demonstrate for the first time, simultaneously effect of electron capture time and injected current polarization on TCDR and NSFI. According to our result, TCDR and NSFI increases by simultaneously electron capture time reduction and increasing of injected current polarization. This increase in TCDR and NSFI leads to lower power consumption and enhances the lasers dynamic performance. Maximum obtained TCDR and NSFI value is 0.353 and 0.90, respectively. Spin-up optical gain term increases by simultaneously rising of levels occupancies probability by spin-up electrons in QD and NH photon occupancies. Maximum obtained Spin-up optical gain 17.70. A very interesting emerging field is lasers based on colloidal

semiconductor QDs typically II–VI, such as CdS, CdSe, ZnSe, and ZnTe [27, 28,29].by providing practical paths to new spin-based devices, we expect that studies of spinlasers will also offer motivation to understanding of spin transport and magnetism.

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